

## Implication recap

“ $P$  implies  $Q$ ” or “if  $P$ , then  $Q$ ” has the following truth table:

$P$	$Q$	$P \implies Q$
T	T	T
T	F	F
F	T	T
F	F	T

You can rephrase “ $P$  implies  $Q$ ” as “ $P$  is a *sufficient condition* for  $Q$ ” or as “ $Q$  is a *necessary condition* for  $P$ .”

## Contrapositive

Logically equivalent to the implication  $P \implies Q$  is the implication  $(\neg Q) \implies (\neg P)$ , called the *contrapositive*.

Example: “If it is Tuesday, then Math 220 meets.” The contrapositive statement is, “If Math 220 is not meeting, then it is not Tuesday.”

$P$	$Q$	$P \implies Q$	$\neg Q$	$\neg P$	$(\neg Q) \implies (\neg P)$
T	T	T	F	F	T
T	F	F	T	F	F
F	T	T	F	T	T
F	F	T	T	T	T

## Converse

The *converse* of  $P \implies Q$  is the statement  $Q \implies P$ , not logically equivalent.

“If it is Tuesday, then Math 220 meets” means something different from “If Math 220 meets, then it is Tuesday.”

# Biconditional

The conjunction of a statement and the converse is the *biconditional*  $P \iff Q$ , “ $P$  if and only if  $Q$ ,” or  $(P \implies Q) \wedge (Q \implies P)$ .

$P \iff Q$  means “ $Q$  is necessary and sufficient for  $P$ .”

## Assignment to hand in next time

Type up a solution to Exercise 17 on page 37 in complete sentences.