Name: Group $\square$

1. Find the general solution of the homogeneous, linear, second order differential equation $\frac{d^{2} y}{d x^{2}}-4 \frac{d y}{d x}+3 y=0$.
2. Find a particular solution of the non-homogeneous differential equation $\frac{d^{2} y}{d x^{2}}-4 \frac{d y}{d x}+3 y=6 x-5$ by the method of undetermined coefficients.
3. By using the previous parts, write down the general solution of the non-homogeneous differential equation $\frac{d^{2} y}{d x^{2}}-4 \frac{d y}{d x}+3 y=6 x-5$.
4. Using the previous part, find the solution of the non-homogeneous differential equation $\frac{d^{2} y}{d x^{2}}-4 \frac{d y}{d x}+3 y=6 x-5$ that satisfies the pair of initial conditions $y(0)=5$ and $y^{\prime}(0)=14$.
5. Check your answer to the previous part: if you plug the solution back into the differential equation $\frac{d^{2} y}{d x^{2}}-4 \frac{d y}{d x}+3 y=6 x-5$, does it really work?
