## Comprehensive final examination

- 12:30-2:30 on Friday afternoon, December 8, in this room.
- Please bring your own paper to work on.

What did we cover this semester?
Chapter I: Sections 1-2 and 4-8
Chapter II: Sections 2-7
Chapter III: Sections 1-3
Chapter IV: Sections 1-4
Chapter V: Sections 1 and 3-4
Chapter VI: Section 1
Chapter VII: Sections 1 and 3

## Announcements / reminders

- Extra office hours this week: Wednesday and Thursday afternoon, 2:00-3:55.
- Some old exams and solutions are posted.
- Please complete the course evaluation. Thanks if you have already done so.


## Some review exercises

1. Determine the minimum value of $\left|\sin \left(\frac{\pi}{2}+i y\right)\right|$ when $y$ runs over all real numbers.
2. Suppose $w=\frac{1+z}{1-z}$. Determine the image in the $w$-plane of $\{z:|z|<1\}$, the unit disk in the $z$-plane.
3. What are all the possible values of the line integral $\int_{C} \frac{1}{z^{2}+1} d z$ when $C$ varies over all possible closed paths?
4. Can you find a rational function $f$ with the property that the Taylor series of $f$ with center 2 has radius of convergence equal to 3 and the Taylor series of $f$ with center -2 has radius of convergence equal to 1 ?
